

*Precise measurement of  
hadronic tau-decays  
with eta mesons at Belle*

2008.9.23

*Tau08*

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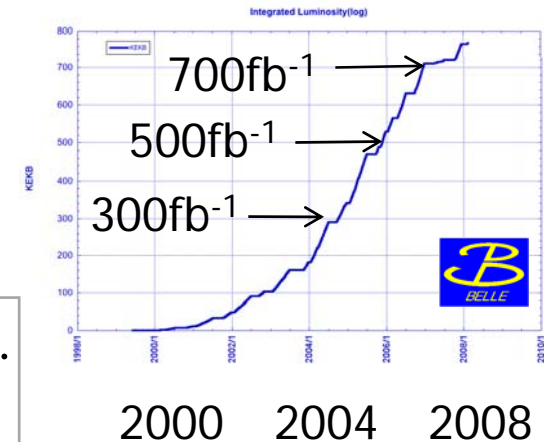
*K. Inami and Belle collaboration*



# Introduction

😊 Belle detector has collected the  $\tau$ -pair data with **the highest statistics in the world**.

At the present, about  $850\text{fb}^{-1}$  of data have been collected. It corresponds to  $7.0 \times 10^8$   $\tau$ -pairs!



😊  $\tau$  hadronic decay from  $e^+e^- \rightarrow \tau^+\tau^-$  process is **very clean**.

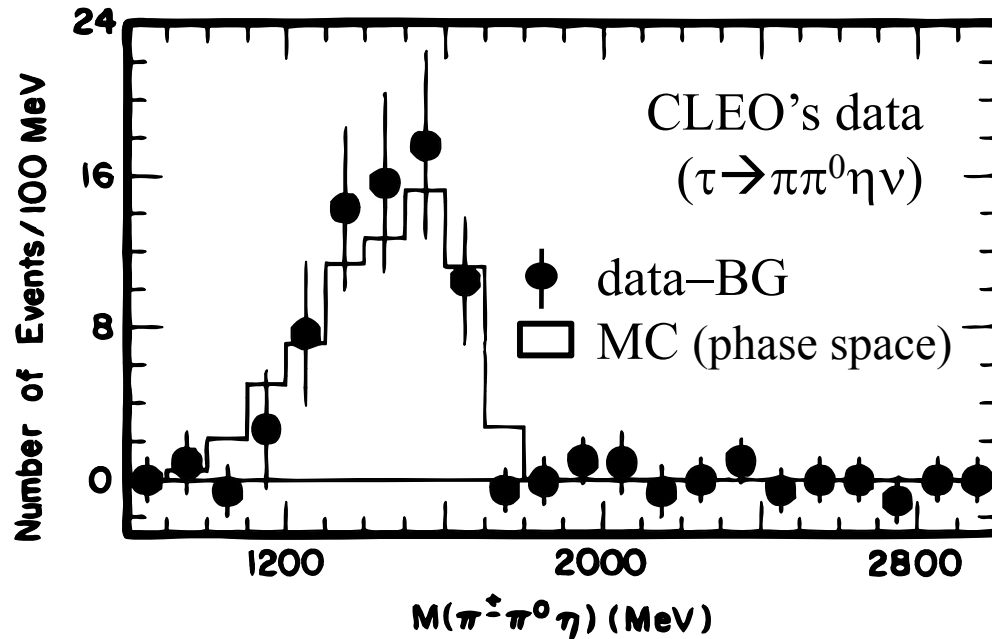
😊  $\tau$  hadronic decay is good for studying low energy QCD phenomena.

- Test of the Vector dominance model (VDM)
- Test of the conserved vector current (CVC)

through BR and mass spectra in  $\tau \rightarrow \pi \pi^0 \eta \nu$  decay.

# Motivation

We can test CVC through  $\tau \rightarrow \pi\pi^0\eta\nu$  decay.



CLEO collaboration has already studied  $\tau \rightarrow \pi\pi^0\eta\nu$  decay, but experimental statistics was very limited.



$M_{\pi\pi^0\eta}$  is not distinguishable from phase space alone.

By using a 100 times larger data sample than that of CLEO, we can test CVC from not only  $BR(\tau \rightarrow \pi\pi^0\eta\nu)$  but also  $M_{\pi\pi^0\eta}$ .

# Contents

- Event selection
- $\eta$  with 1 charged track
  - $\tau^- \rightarrow K^- \eta \nu, K^- \pi^0 \eta \nu, \pi^- \pi^0 \eta \nu$  with  $\eta \rightarrow \gamma \gamma$
  - Cross check for  $\tau^- \rightarrow K^- \eta (\rightarrow \gamma \gamma) \nu$ 
    - $\tau^- \rightarrow K^- \eta (\rightarrow \pi \pi \pi^0) \nu$
  - Result
- $\eta$  with  $K_S$ 
  - $\tau^- \rightarrow \pi^- K_S \eta \nu, K^- K_S \eta \nu$
  - Result
- $\tau^- \rightarrow K^{*-} \eta \nu$  study
  - $\tau^- \rightarrow K^- \pi^0 \eta \nu, \pi^- K_S \eta \nu$
- Discussion
  - Compare with the previous result
  - Compare with the theoretical predictions
  - Check for CVC

# Event selection

Data set :  $490\text{fb}^{-1}$

## tag side

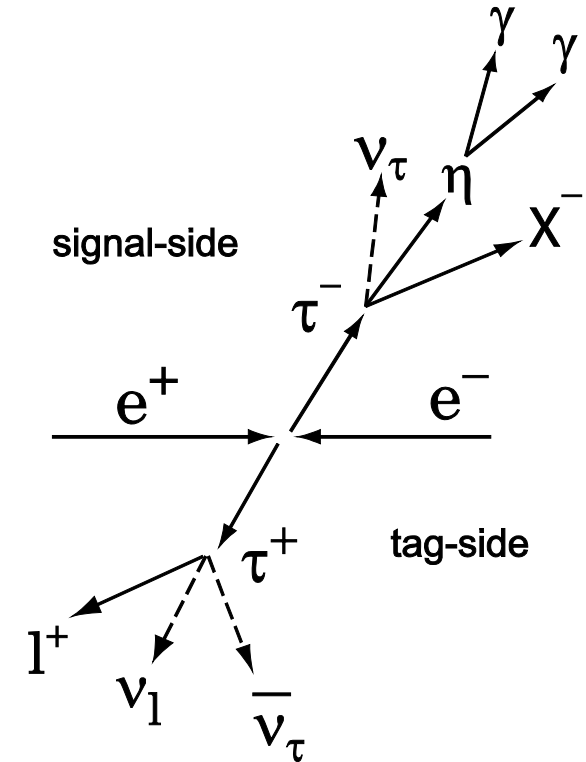
- $\tau^+ \rightarrow l^+ \nu \nu$ ; 1 charged track
- Require lepton (to suppress  $q\bar{q}$  events)

## signal side

- $\tau^- \rightarrow X^- \eta \nu$ ; 1 or 3 charged tracks
  - $X^-$  :  $K^-$ ,  $K^-\pi^0$ ,  $\pi^-\pi^0$ ,  $\pi^-K_S$ ,  $K^{*-}$  (892) systems
  - $\eta \rightarrow \pi^+\pi^-\pi^0$  is used for  $\tau^- \rightarrow K^-\eta\nu$  decay only
    - $\pi^0 \rightarrow \gamma\gamma$  :  $105 < M_{\gamma\gamma} < 165 \text{MeV}/c^2$

## other requirements

- $\pi^0$  veto
- missing momentum

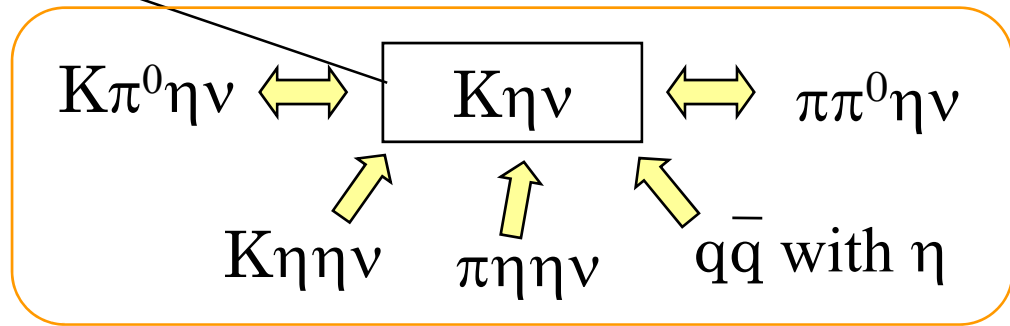
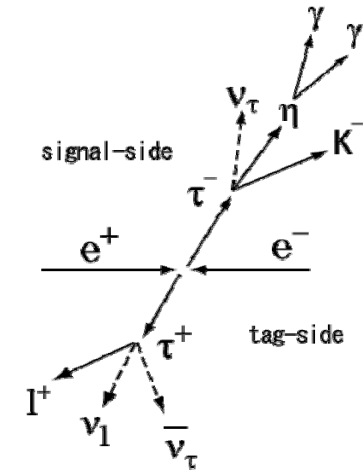
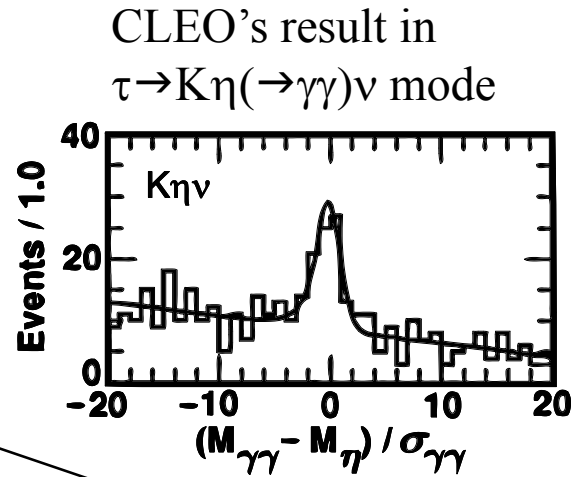
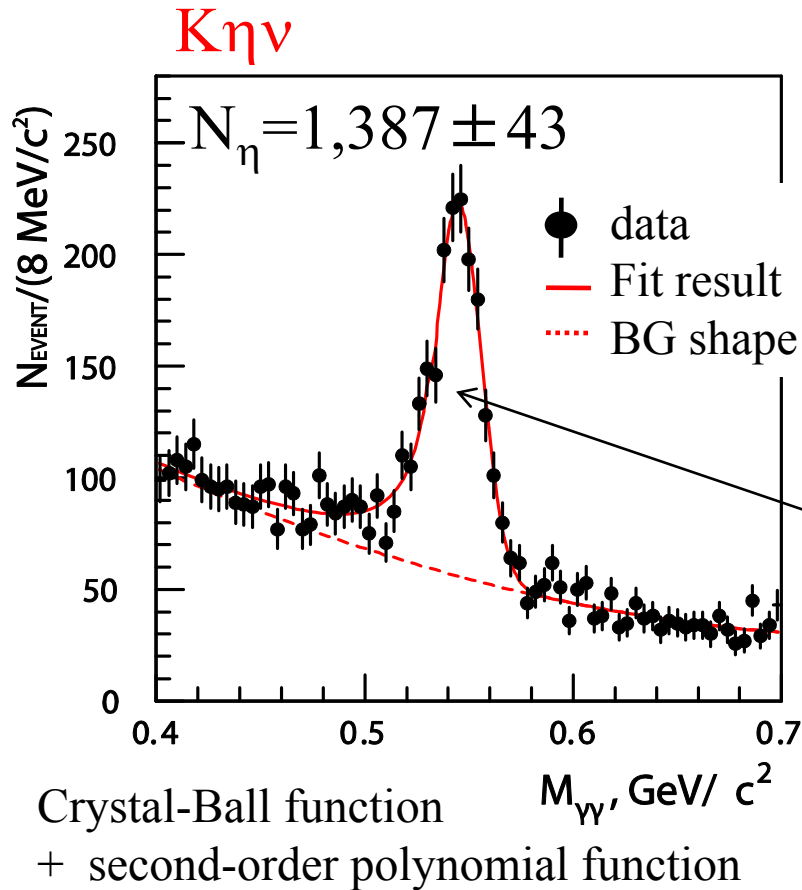


( $X^-$  denotes  $K^-$ ,  $K^-\pi^0$ ,  $\pi^-\pi^0$ ,  $\pi^-K_S$ ,  $K^{*-}$ (892) systems)  
 $\pi^0 \rightarrow \gamma\gamma$   
 $K_S \rightarrow \pi^+\pi^-$   
 $K^{*-}$ (892)  $\rightarrow K_S\pi^-$

The number of signal events is evaluated from  $\eta$  mass or  $K^*$  mass distribution.

*$\eta$  with 1 charged track*

# $\tau^- \rightarrow K^- \eta \nu$ ( $\eta \rightarrow \gamma\gamma$ )

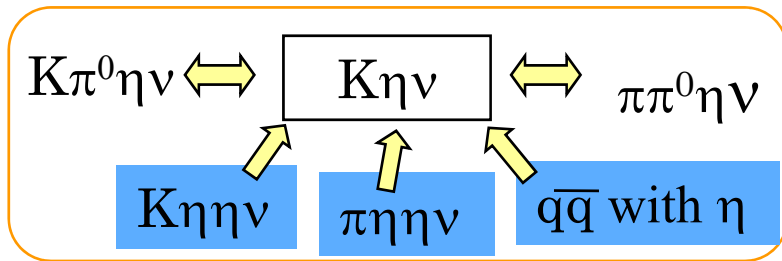


Main  $\eta$ -peaking BG components for  $\tau \rightarrow K\eta\nu$  are  $\tau \rightarrow K\pi^0\eta\nu$ ,  $\pi\pi^0\eta\nu$ ,  $ee \rightarrow q\bar{q}$ .

By evaluating the number of  $\eta$ ,  $\text{Br}(\tau \rightarrow K\eta\nu)$  is measured.

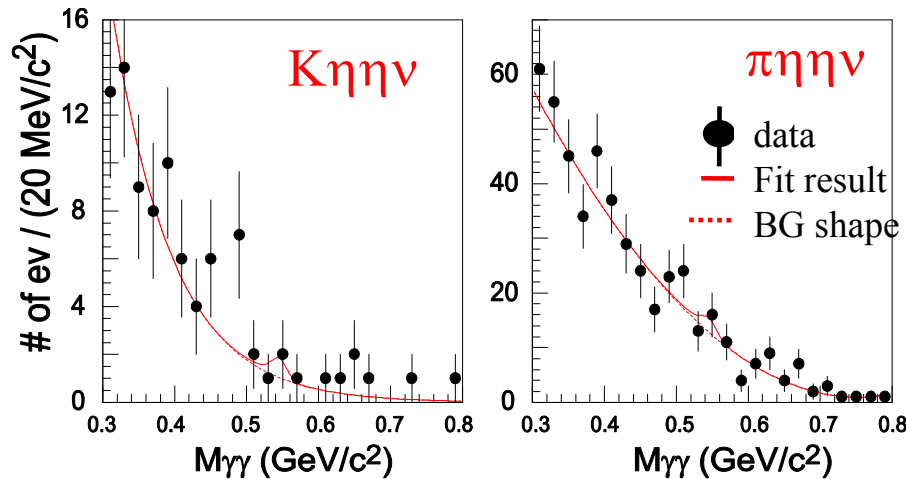
But the signal  $\eta$  peak is contaminated by  $K\pi^0\eta\nu$ ,  $\pi\pi^0\eta\nu$  etc.

# Peaking BG : $K\eta\eta\nu, \pi\eta\eta\nu, q\bar{q}$ ( $\eta \rightarrow \gamma\gamma$ )



We estimate the contamination of  $K\eta\eta$ ,  $\pi\eta\eta$  and  $q\bar{q}$  to the signal from data.

$\tau^- \rightarrow K^- \eta \eta \nu, \pi^- \eta \eta \nu$  (Special selection of  $K/\pi$   $\eta\eta$  candidates)



Crystal-Ball function + second-order polynomial function

$BR(\tau \rightarrow K\eta\eta\nu) < 3.0 \times 10^{-6}$  @90%C.L.

$BR(\tau \rightarrow \pi\eta\eta\nu) < 7.4 \times 10^{-6}$  @90%C.L.

The contamination to the signal mode **can be ignored.**

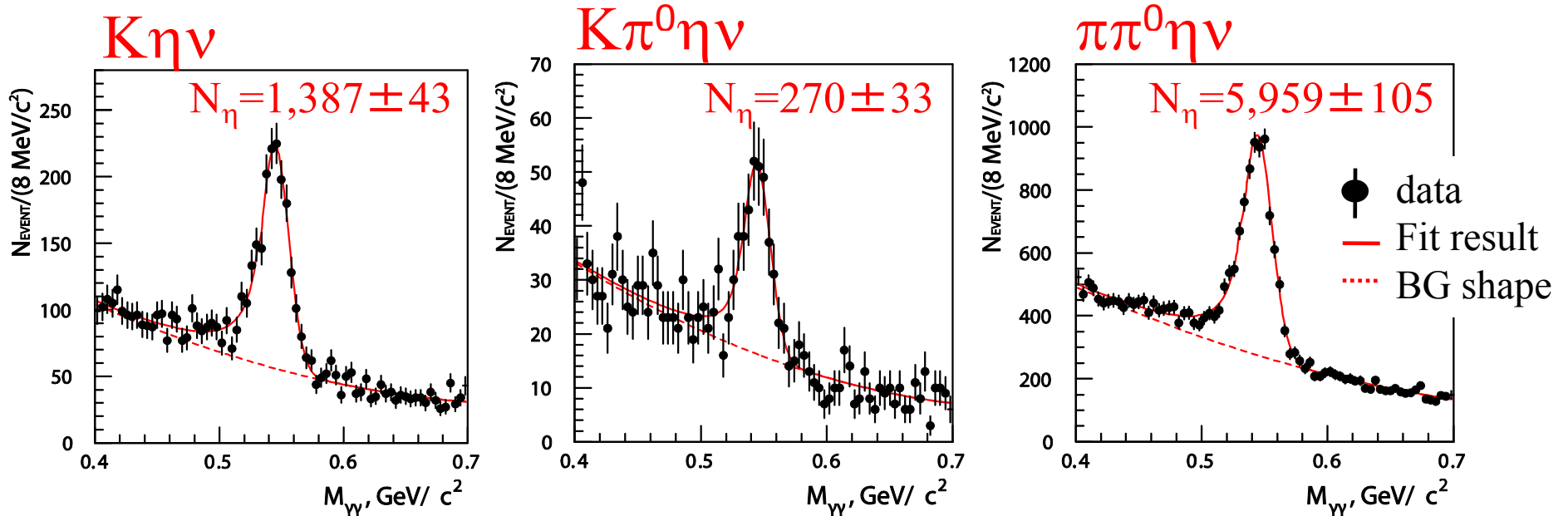
## $q\bar{q}$ with $\eta$

evaluate  $q\bar{q}$  events by comparing data and  $q\bar{q}$ MC with  $q\bar{q}$  enriched selection ( $M_{\text{tag}} > M_{\tau}$ , no  $M_{\text{sig}} < M_{\tau}$ ,  $P_{e/\mu} < 0.8$ )

$q\bar{q}$  contamination is evaluated to 2.8%, 10% and 3.6% of the signal candidates,  $N_{\eta}$ , in the  $\tau \rightarrow K\eta\nu$ ,  $\tau \rightarrow K\pi^0\eta\nu$  and  $\tau \rightarrow \pi\pi^0\eta\nu$  decay, respectively.



# $\tau^- \rightarrow K^- \eta \nu, \pi^- \pi^0 \eta \nu, K^- \pi^0 \eta \nu$ ( $\eta \rightarrow \gamma\gamma$ )

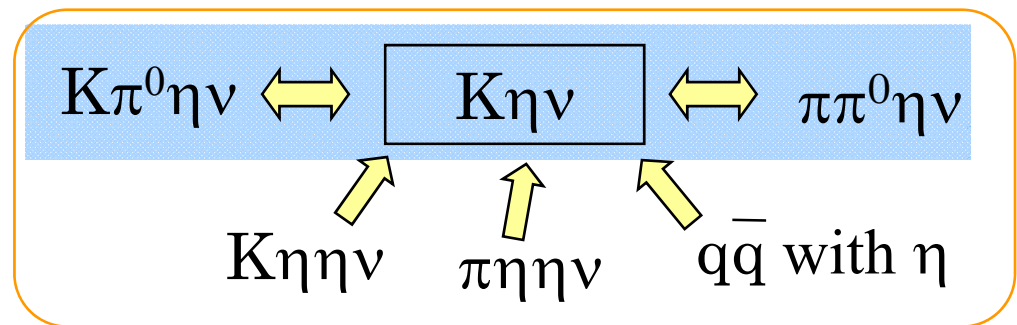


$$N_j = 2N_{\tau\tau} \sum_i \varepsilon_j^i B_i$$

( $i, j = K^- \eta \nu, K^- \pi^0 \eta \nu, \pi^- \pi^0 \eta \nu$ )

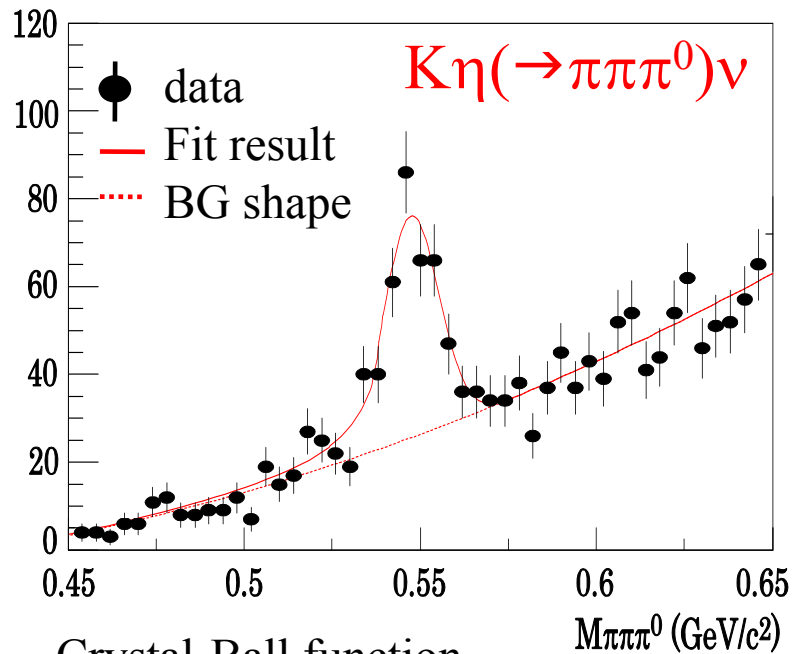
efficiency  $\varepsilon_j^i$

Branching ratio  $B_i$



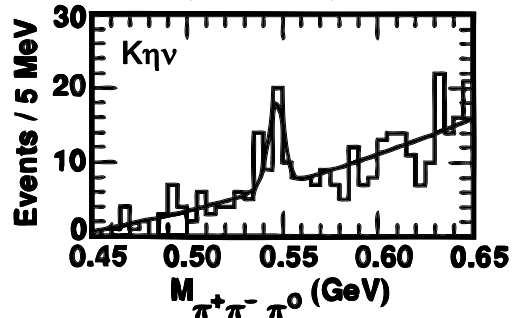
- estimate  $\eta$  yield  $\Rightarrow$  fit Crystal Ball function for  $\gamma\gamma$  mass distributions
- Simultaneously, their BR are evaluated.
- We can suppress systematic errors for each modes

# Cross check for $\tau^- \rightarrow \text{K}^- \eta \nu$ ( $\eta \rightarrow \gamma\gamma$ )



Crystal-Ball function  
+ second-order polynomial function

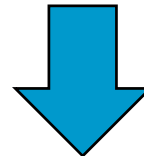
CLEO's result in  
 $\tau \rightarrow \text{K} \eta (\rightarrow \pi\pi\pi^0) \nu$  mode



As a cross check for  $\tau \rightarrow \text{K} \eta (\rightarrow \gamma\gamma) \nu$  mode, we measure the BR of  $\tau \rightarrow \text{K} \eta (\rightarrow \pi\pi\pi^0) \nu$  mode.

$$\begin{aligned} \text{BR}(\tau \rightarrow \text{K} \eta \nu) &= (1.60 \pm 0.15 \pm 0.10) \times 10^{-4} @ \eta \rightarrow \pi^+ \pi^- \pi^0 \\ &= (1.57 \pm 0.05 \pm 0.09) \times 10^{-4} @ \eta \rightarrow \gamma\gamma \end{aligned}$$

We find a good agreement between these two results.



Our measurements have self consistency!

# Systematic study

Signal modes		$K\eta\nu$	$K\pi^0\eta\nu$	$\pi\pi^0\eta\nu$	$K\eta\nu$
Items		$\eta \rightarrow \gamma\gamma$			$\eta \rightarrow \pi\pi\pi^0$
BG subtraction	$K\eta\nu$	--	0.6	$1.8 \times 10^{-3}$	--
	$K\pi^0\eta\nu$	0.3	--	$4.2 \times 10^{-2}$	0.4
	$\pi\pi^0\eta\nu$	$7.5 \times 10^{-2}$	3.3	--	0.1
	$\pi\pi^0\pi^0\eta\nu$	--	--	0.4	--
	$q\bar{q}$	1.5	6.0	0.5	1.5
Detection efficiency	$K/\pi$ / lepton-ID	3.3/2.3	2.2/2.8	1.0/2.6	2.8/2.6
	Tracking	1.3	1.3	1.3	3.3
	$\pi^0$ / $\eta \rightarrow \gamma\gamma$	--/2.0	2.0/2.0	2.0/2.0	2.0/--
	$\pi^0$ veto	2.8	2.8	2.8	--
stat. error of signal MC		0.5	1.7	0.5	1.3
BR( $\tau \rightarrow \pi\pi\pi^0$ )		--	--	--	1.6
Luminosity		1.4			
$\sigma(e^+e^- \rightarrow \tau^+\tau^-)$		0.3			
total		5.9%	9.1%	5.3%	6.2%

By evaluating cross-feed BG simultaneously, we can suppress systematic errors.

# Results ( $\eta$ with 1 charged track)

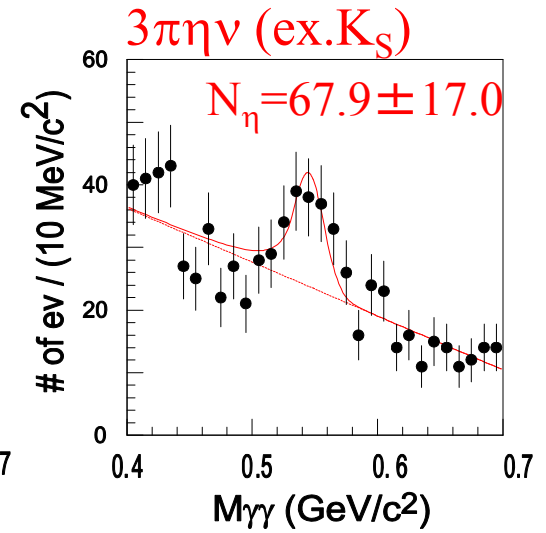
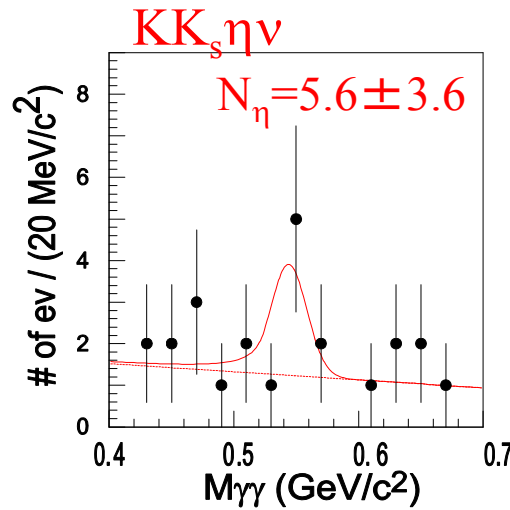
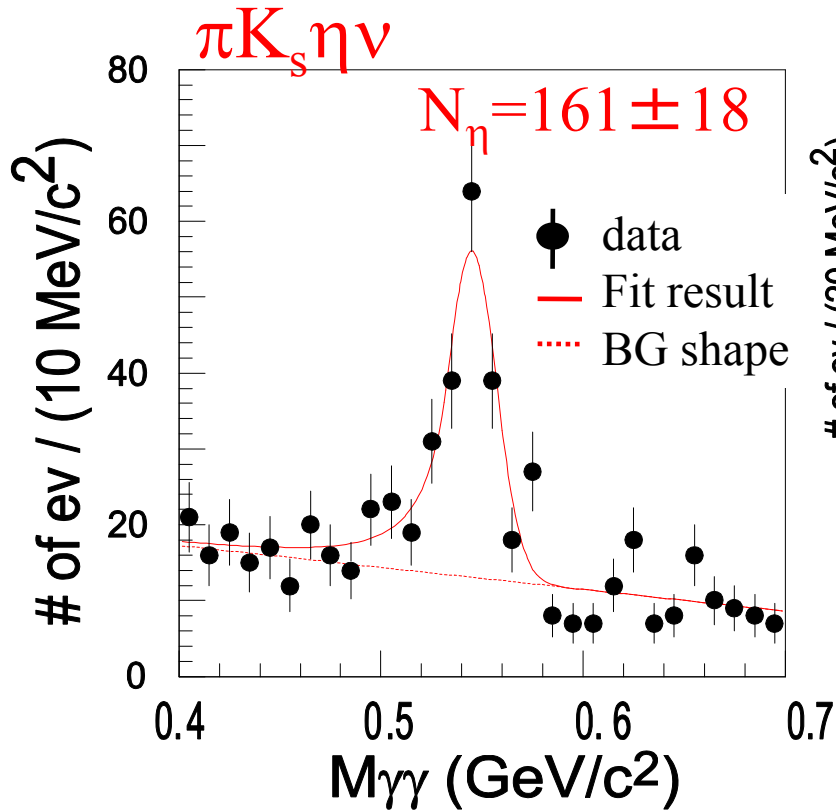
Belle preliminary

Modes	Our Br or upper limit	
$\tau \rightarrow K\eta\nu$ (combined)	$(1.58 \pm 0.05 \pm 0.09) \times 10^{-4}$	← combined ] consistent
$\tau \rightarrow K\eta\nu$ (@ $\eta \rightarrow \gamma\gamma$ )	$(1.57 \pm 0.05 \pm 0.09) \times 10^{-4}$	
$\tau \rightarrow K\eta\nu$ (@ $\eta \rightarrow \pi\pi\pi^0$ )	$(1.60 \pm 0.15 \pm 0.10) \times 10^{-4}$	
$\tau \rightarrow K\pi^0\eta\nu$	$(4.6 \pm 1.1 \pm 0.4) \times 10^{-5}$	
$\tau \rightarrow \pi\pi^0\eta\nu$	$(1.35 \pm 0.03 \pm 0.07) \times 10^{-3}$	
$\tau \rightarrow K\eta\eta\nu$	$< 3.0 \times 10^{-6}$ @90% C.L.	
$\tau \rightarrow \pi\eta\eta\nu$	$< 7.4 \times 10^{-6}$ @90% C.L.	

The self consistency shows that our results are reliable.

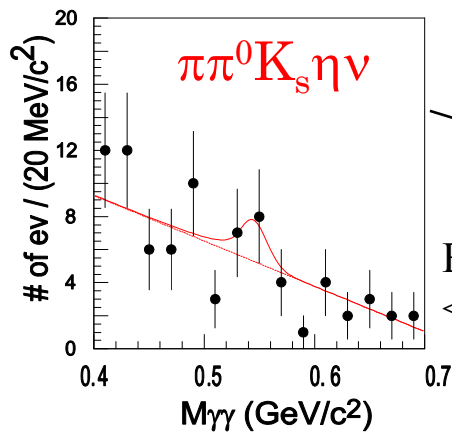
*$\eta$  with  $K_S$*

# $\tau^- \rightarrow \pi^- K_s \eta \nu$

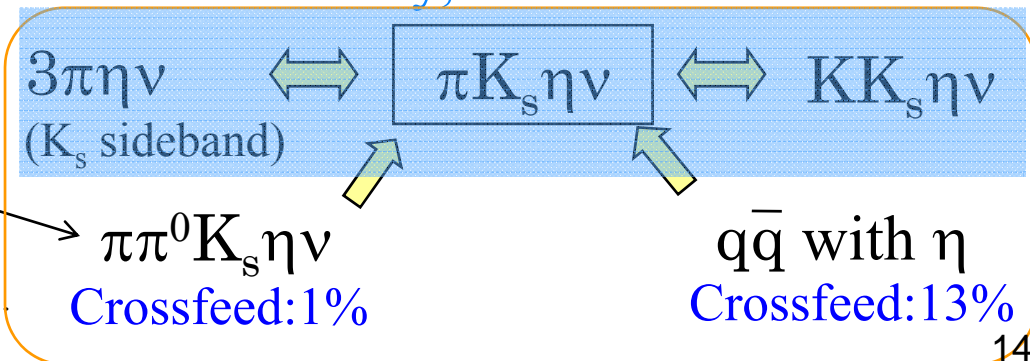


$$N_j = 2N_{\tau\tau} \sum_i \overset{\text{efficiency}}{\varepsilon_j^i} \underset{\text{Branching ratio}}{B_i} \quad \begin{matrix} (i,j \\ = \pi^- K_s \eta \nu, K^- K_s \eta \nu, 3\pi^\pm \eta \nu) \end{matrix}$$

Simultaneously, these BR are evaluated.



$BR(\tau \rightarrow \pi\pi^0 K_s \eta \nu)$   
 $< 2.5 \times 10^{-5}$  @90% C.L.



Crystal-Ball function + second-order polynomial function

# Results ( $\eta$ with $K_S$ )

Belle preliminary

Modes	Our Br or upper limit
$\tau \rightarrow \pi K_S \eta \nu$	$(4.4 \pm 0.7 \pm 0.3) \times 10^{-5}$
$\tau \rightarrow K K_S \eta \nu$	$< 4.5 \times 10^{-6}$ @90% C.L.
$\tau \rightarrow \pi \pi^0 K_S \eta \nu$	$< 2.5 \times 10^{-5}$ @90% C.L.

The systematic error for  $\tau \rightarrow \pi K_S \eta \nu$

- Total : 6.4%
- Fitting function : 4.1%

The uncertainty from the fitting function is dominant one

$\tau \rightarrow K^* \eta \nu$  study



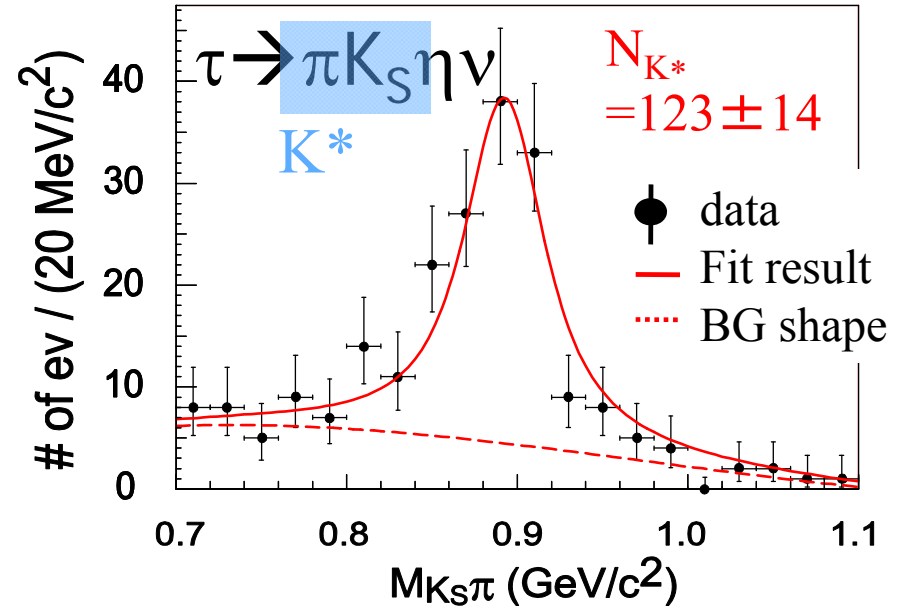
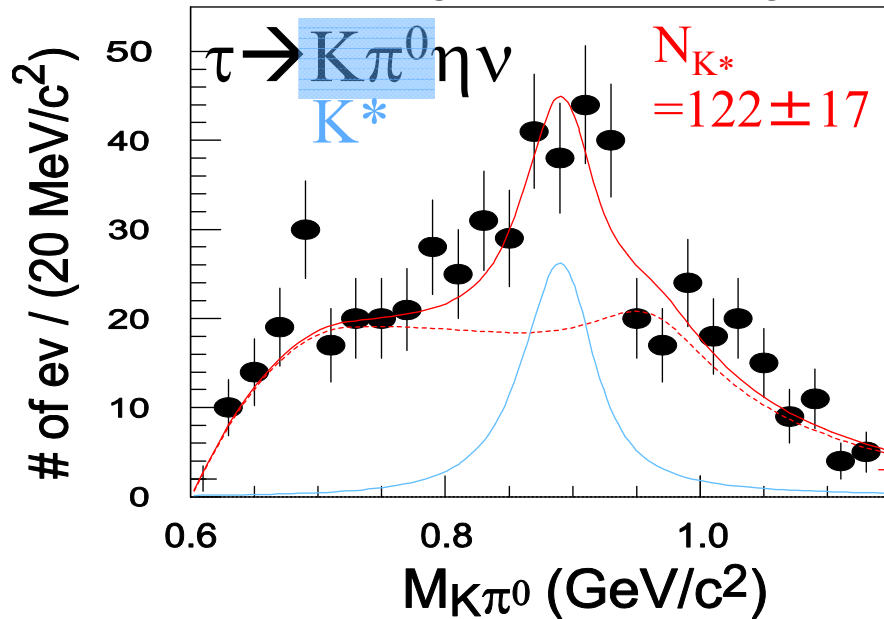
# $\tau^- \rightarrow K^{*-} \eta \nu$

Charged  $K^*(892)$  decays into  $K\pi^0$  or  $\pi K_S$  with same rate because iso-spin relation.

$$\begin{aligned} \text{BR}(\tau \rightarrow K\pi^0 \eta \nu) &= (4.6 \pm 1.1 \pm 0.4) \times 10^{-5} \\ \text{BR}(\tau \rightarrow \pi K_S \eta \nu) &= (4.4 \pm 0.7 \pm 0.3) \times 10^{-5} \end{aligned}$$

This agreement suggests that  $K^*$  is dominant in both modes.

Convolved Breit-Wigner function + bg function



Main BGs in these modes are evaluated from  $M_{\gamma\gamma}$  side bands, respectively.

These fitting results show that  $K^*(892)$  is almost 100% in the final state in both  $\tau \rightarrow K\pi^0 \eta \nu$  and  $\tau \rightarrow \pi K_S \eta \nu$  decays.

# Results ( $\tau^- \rightarrow K^{*-} \eta \nu$ )

Belle preliminary

Modes	Our Br
$\tau \rightarrow K^* \eta \nu$ (combined)	$(1.34 \pm 0.12 \pm 0.09) \times 10^{-4}$
$\tau \rightarrow K^* \eta \nu$ (@ $K^* \rightarrow K \pi^0$ )	$(1.13 \pm 0.17 \pm 0.18) \times 10^{-4}$
$\tau \rightarrow K^* \eta \nu$ (@ $K^* \rightarrow \pi K_S$ )	$(1.46 \pm 0.16 \pm 0.09) \times 10^{-4}$

← combined

consistent

$\tau \rightarrow \pi K_S \eta \nu$  mode plays a role as a cross check for  $\tau \rightarrow K \pi^0 \eta \nu$ .  
The self consistency shows that our results are reliable.

The systematic error for  $\tau \rightarrow K^* \eta \nu$  (@ $K^* \rightarrow K \pi^0$ )

● Total : 16.2% / Fitting function : 15.0%

The systematic error for  $\tau \rightarrow K^* \eta \nu$  (@ $K^* \rightarrow \pi K_S$ )

● Total : 6.4% / Fitting function : 4.1%

The uncertainty from the fitting function is dominant one

# DISCUSSION

# Comparison with previous CLEO results

We obtain precise results in each  $\tau$  decay mode including  $\eta$ .

Belle preliminary

Modes	Our Br( $\times 10^{-3}$ )	CLEO's Br( $\times 10^{-3}$ )	Error ratio $\delta(\text{CLEO})/\delta(\text{Belle})$
$\tau \rightarrow K\eta\nu$	$0.158 \pm 0.005 \pm 0.009$	$0.26 \pm 0.05 \pm 0.05$	7.0
$\tau \rightarrow K\pi^0\eta\nu$	$0.046 \pm 0.011 \pm 0.004$	$0.177 \pm 0.056 \pm 0.071$	7.5
$\tau \rightarrow \pi\pi^0\eta\nu$	$1.35 \pm 0.03 \pm 0.07$	$1.7 \pm 0.2 \pm 0.2$	3.8
$\tau \rightarrow K_S\pi\eta\nu$	$0.044 \pm 0.007 \pm 0.002$	$0.100 \pm 0.035 \pm 0.011$	5.3
$\tau \rightarrow K^*\eta\nu$	$0.134 \pm 0.012 \pm 0.009$	$0.290 \pm 0.080 \pm 0.042$	6.0

Modes	Our Upper limit
$\tau \rightarrow K_S K\eta\nu$	$<4.5 \times 10^{-6}$ @90% C.L.
$\tau \rightarrow K_S \pi\pi^0\eta\nu$	$<2.5 \times 10^{-5}$ @90% C.L.
$\tau \rightarrow K\eta\eta\nu$	$<3.0 \times 10^{-6}$ @90% C.L.
$\tau \rightarrow \pi\eta\eta\nu$	$<7.4 \times 10^{-6}$ @90% C.L.

The central values of our BRs in all modes are lower than those of the CLEO's results.

- Underestimate BG contributions in CLEO
  - Cross feed BG contribution
  - $q\bar{q}$

- High statistics enable us to reliably estimate BG contributions for each mode using data.
- We check the self consistency of BR in several modes.

# Comparison with theoretical predictions

Belle preliminary

Modes	Our Br	Theoretical predictions of Br	
		CVC	Chiral perturbation theory
$\tau \rightarrow K\eta\nu$	$(1.58 \pm 0.05 \pm 0.09) \times 10^{-4}$	-----	$1.2 \times 10^{-4}$ [3], $2.2 \times 10^{-4}$ [5], $1.6 \times 10^{-4}$ [6]
$\tau \rightarrow K\pi^0\eta\nu$	$(4.6 \pm 1.1 \pm 0.4) \times 10^{-5}$	-----	$8.8 \times 10^{-6}$ [3], $7.7 \times 10^{-6}$ [6]
$\tau \rightarrow \pi\pi^0\eta\nu$	$(1.35 \pm 0.03 \pm 0.07) \times 10^{-3}$	$(1.3 \pm 0.2) \times 10^{-3}$ [1], $1.5 \times 10^{-3}$ [2]	$3 \times 10^{-3}$ [3], $1.4 \times 10^{-3}$ [4], $1.9 \times 10^{-3}$ [5]
$\tau \rightarrow K_s\pi\eta\nu$	$(4.4 \pm 0.7 \pm 0.2) \times 10^{-5}$	-----	$1.1 \times 10^{-5}$ [3], $0.9 \times 10^{-5}$ [6]
$\tau \rightarrow K^*\eta\nu$	$(1.34 \pm 0.12 \pm 0.09) \times 10^{-4}$	-----	$1.0 \times 10^{-4}$ [5]

Modes	Our Upper limit	Theoretical predictions of Br	
		CVC	Chiral perturbation theory
$\tau \rightarrow K_s K\eta\nu$	$< 4.5 \times 10^{-6}$ @90% C.L.	-----	$1.6 \times 10^{-7}$ [3], $1.4 \times 10^{-7}$ [6]
$\tau \rightarrow K_s \pi\pi^0\eta\nu$	$< 2.5 \times 10^{-5}$ @90% C.L.	-----	-----
$\tau \rightarrow K\eta\eta\nu$	$< 3.0 \times 10^{-6}$ @90% C.L.	-----	$1.6 \times 10^{-9}$ [3], $7.0 \times 10^{-9}$ [6]
$\tau \rightarrow \pi\eta\eta\nu$	$< 7.4 \times 10^{-6}$ @90% C.L.	-----	$1.1 \times 10^{-9}$ [3]

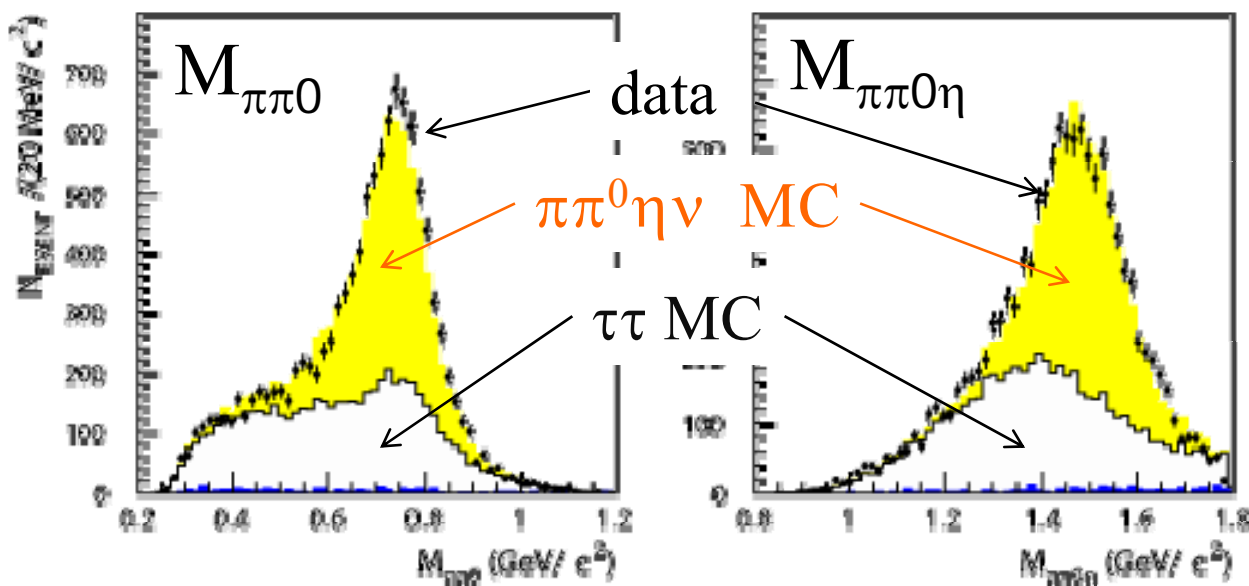
- [1]S.I.Eidelman, PLB 257 (1991) 437  
 [2]F.J.Gilman, PRD 35 (1987) 3541  
 [3]A.Pich, PLB 196 (1987) 561  
 [4]E.Braaten, PRD 36 (1987) 2188  
 [5]B.A.Li, PRD 55 (1997) 1436  
 [6]G.J.Aubrecht, PRD 24 (1981) 1318

- The CVC prediction of  $BR(\tau \rightarrow \pi\pi^0\eta\nu)$  **agrees well** with our result. (our result is more precise)
- High precision of our experiment will allow to discriminate between different theoretical models.

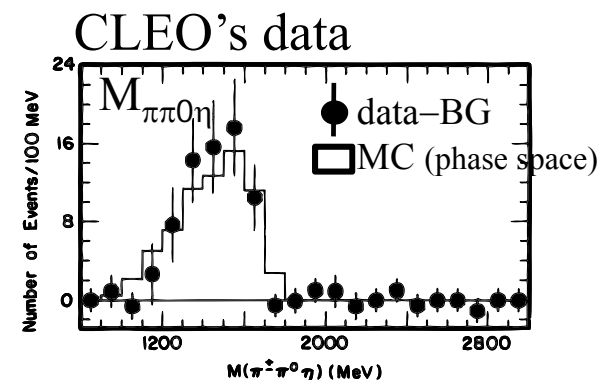
# Check for CVC

Belle preliminary

$\tau \rightarrow \pi\pi^0\eta\nu$  MC generator is designed based on  $\sigma(e^+e^- \rightarrow \pi^+\pi^-\eta)$  measured more than 10 years ago, assuming CVC.



The distributions for the observed data and MC agree well.



$e^+e^- \rightarrow \text{hadrons}$

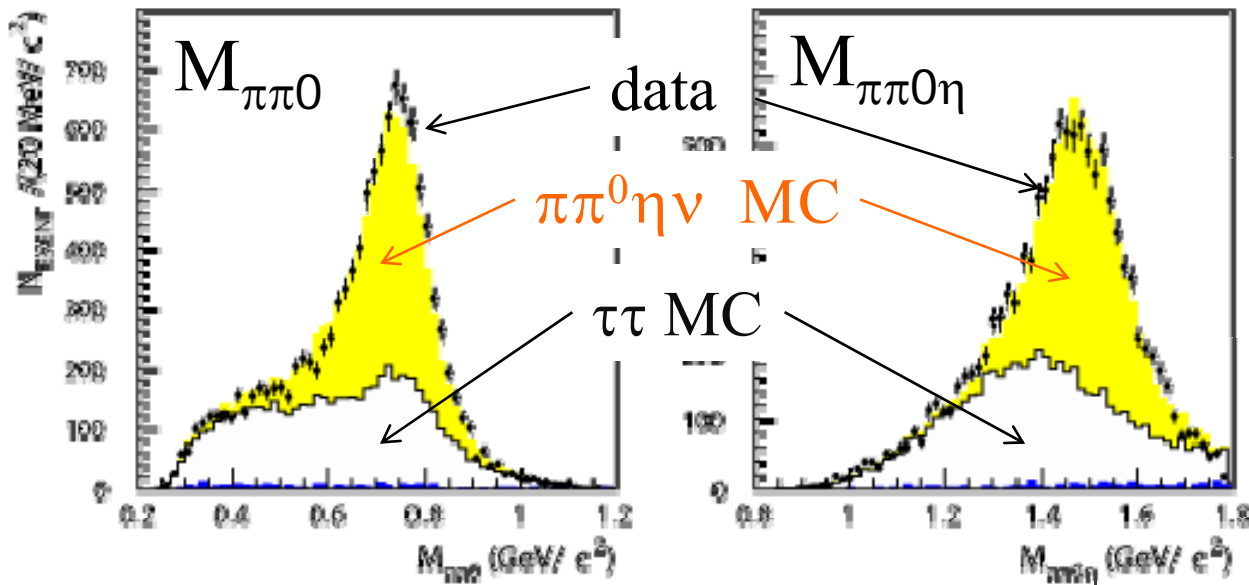
CVC →

$\tau^- \rightarrow \text{hadrons} + \nu$

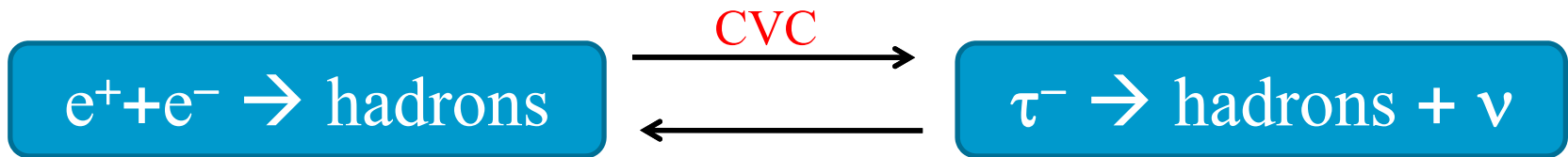
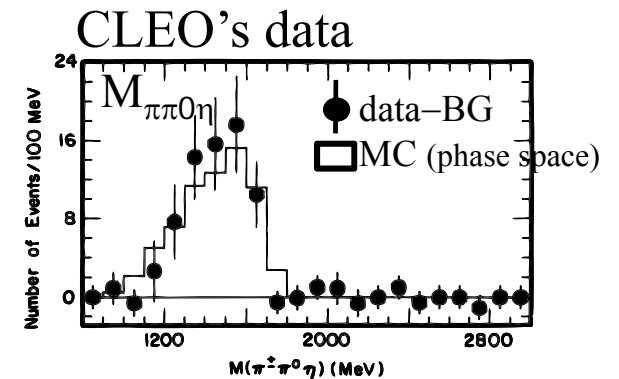
# Check for CVC

Belle preliminary

$\tau \rightarrow \pi\pi^0\eta\nu$  MC generator is designed based on  $\sigma(e^+e^- \rightarrow \pi^+\pi^-\eta)$  measured more than 10 years ago, assuming CVC.



The distributions for the observed data and MC agree well.



Check in high accuracy

Now, we can compare  $\tau \rightarrow \text{hadrons} + \nu$  and  $e^+e^- \rightarrow \text{hadrons}$  with high accuracy to check CVC.

# Summary



We perform a high-precision study of  $\tau \rightarrow X + \eta \nu$  based on  $4.5 \times 10^8$   $\tau$ -pairs.

Improve the uncertainty of  $\text{BR}(\tau \rightarrow X + \eta \nu)$  by a factor of **3.8~7.5** times

- $\text{BR}(\tau \rightarrow K \eta \nu) = (1.58 \pm 0.05 \pm 0.09) \times 10^{-4}$
- $\text{BR}(\tau \rightarrow K \pi^0 \eta \nu) = (4.6 \pm 1.1 \pm 0.4) \times 10^{-5}$
- $\text{BR}(\tau \rightarrow \pi \pi^0 \eta \nu) = (1.35 \pm 0.03 \pm 0.07) \times 10^{-3}$
- $\text{BR}(\tau \rightarrow K_s \pi \eta \nu) = (4.4 \pm 0.7 \pm 0.2) \times 10^{-5}$
- $\text{BR}(\tau \rightarrow K^* \eta \nu) = (1.34 \pm 0.12 \pm 0.09) \times 10^{-4}$
- $\text{BR}(\tau \rightarrow K_s K \eta \nu) < 4.5 \times 10^{-6}$  @90% C.L.
- $\text{BR}(\tau \rightarrow K_s \pi \pi^0 \eta \nu) < 2.5 \times 10^{-5}$  @90% C.L.
- $\text{BR}(\tau \rightarrow K \eta \eta \nu) < 3.0 \times 10^{-6}$  @90% C.L.
- $\text{BR}(\tau \rightarrow \pi \eta \eta \nu) < 7.4 \times 10^{-6}$  @90% C.L.

Belle preliminary

Our results are reliable

- BG estimation
  - All  $\tau\tau$  BGs are evaluated ourselves.
  - $q\bar{q}$  BG are estimated by data.
- The self consistency in  $\tau \rightarrow K \eta \nu$  and  $\tau \rightarrow K^* \eta \nu$  branching ratios

Check CVC with high accuracy

- The precise measurement of  $\tau \rightarrow \pi \pi^0 \eta \nu$  decay
- High statistical data
- ➡ The CVC prediction of  $\text{BR}(\tau \rightarrow \pi \pi^0 \eta \nu)$  **agrees well** with our result.
  - $M_{\pi\pi^0}$  and  $M_{\pi\pi^0\eta}$  distributions show that CVC model **works well** at this level.



# BACK UP

# MC generation

For these modes, the efficiency is determined assuming V-A interaction and the phase space decay for the hadronic system.

$$\tau \rightarrow K \eta \nu$$

$$\tau \rightarrow K \pi^0 \eta \nu$$

$$\tau \rightarrow K \eta \eta \nu$$

$$\tau \rightarrow \pi \eta \eta \nu$$

$$\tau \rightarrow K_s \pi \eta \nu$$

$$\tau \rightarrow K_s K \eta \nu$$

$$\tau \rightarrow K_s \pi \pi^0 \eta \nu$$

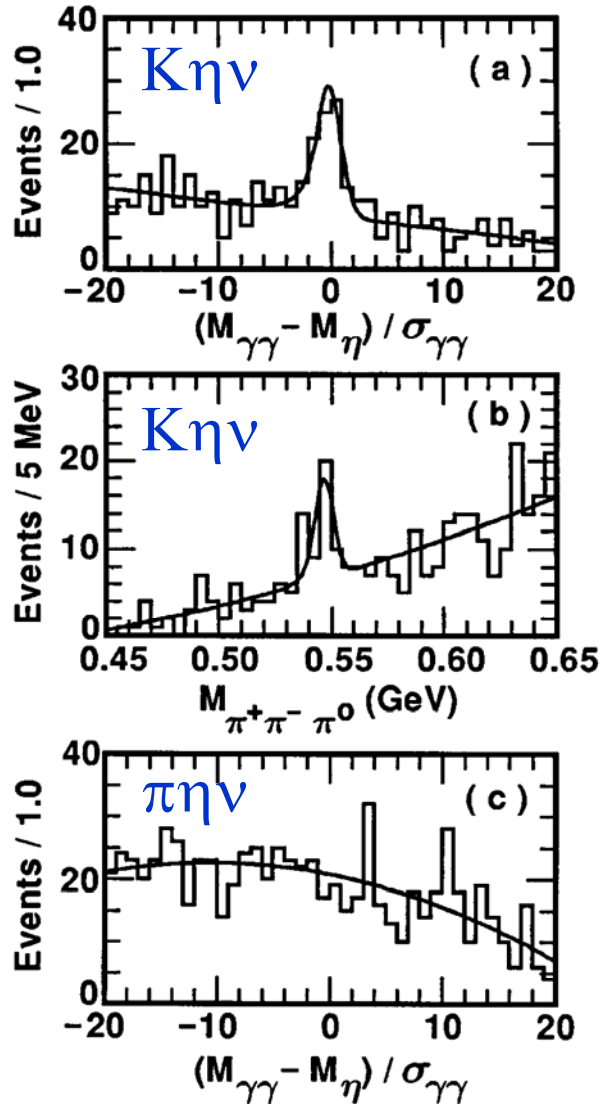
$$\tau \rightarrow K^* \eta \nu$$

# CLEO's results

**Phys. Rev. Lett. 76, 4119–4123 (1996)**

TABLE I. Summary of signals, backgrounds, detection efficiencies, and branching fractions. All errors are statistical.

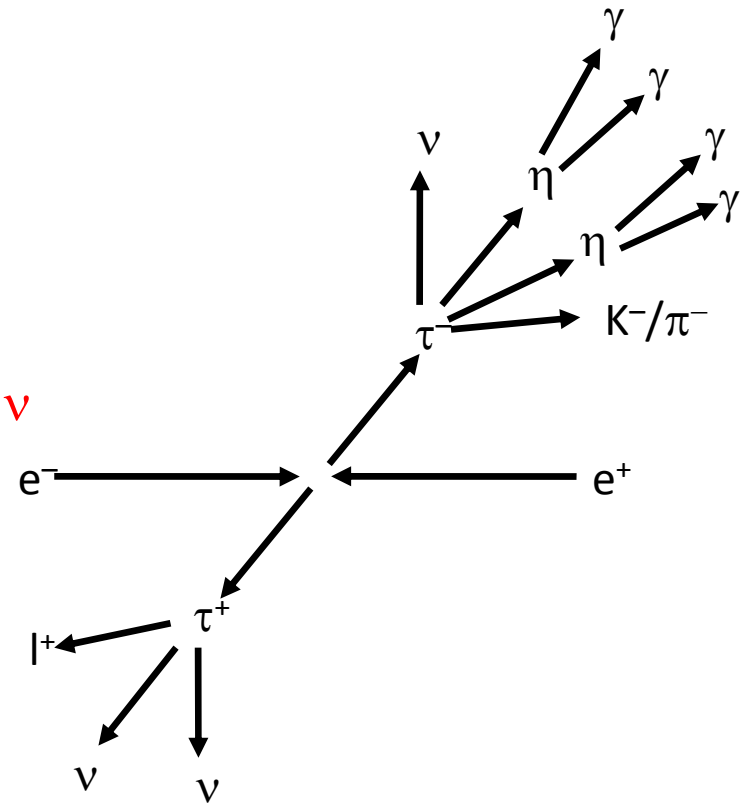
	$K^- \gamma \gamma$	$K^- \pi^+ \pi^- \pi^0$	$\pi^- \gamma \gamma$
$\eta$ signal	$61 \pm 11$	$24 \pm 7$	$0_{-0}^{+5.3}$
$q\bar{q}$	$8.2 \pm 3.8$	$5.9 \pm 3.1$	$2.7 \pm 1.9$
$\pi^- \pi^0 \eta$	$3.2 \pm 0.8$	$3.8 \pm 1.0$	$3.9 \pm 0.9$
Cross-feed eff (%)	$1.3 \pm 0.1$	$0.8 \pm 0.1$	$0.8 \pm 0.1$
Eff (%)	$7.6 \pm 0.1$	$3.9 \pm 0.1$	$3.5 \pm 0.1$
$B (10^{-4})$	$2.6 \pm 0.6$	$2.5 \pm 1.3$	$0_{-0}^{+0.62}$



- Integrated luminosity of  $3.5 \text{ fb}^{-1}$  was analyzed.
- Totally, 50 events were observed.
- They assume branching ratio of  $K\pi^0\eta\nu$ ,  $\sim 10^{-6}$  from theory
- $\text{Br}(K\eta\nu) = (2.6 \pm 0.5 \pm 0.4) \times 10^{-4}$   
 $\text{Br}(\pi\eta\nu) < 1.4 \times 10^{-4}$

# Event selection for $K\eta\eta\nu$ and $\pi\eta\eta\nu$

- 1-1 topology,  $\eta \rightarrow \gamma\gamma$
- Signal-side
  - $N_\gamma = 4$
  - K/ $\pi$  ID for track
  - $\pi^0$  veto for  $\gamma_\eta$
  - $P_\eta^\tau$  selection in " $\tau$  rest frame" for  $K\eta\eta\nu$
  - $E_\gamma > 0.1$  (0.3) GeV for  $K\eta\eta\nu$  ( $\pi\eta\eta\nu$ )
- Lepton tag



# Event selection for $K_S\pi\eta\nu$

- $\tau^- \rightarrow K_S (\rightarrow \pi^- \pi^+) \pi^- \eta \nu$
- 3-1 topology
- Signal side
  - $N_\gamma = 2$
  - $0.45 < M_{\pi\pi} < 0.55$ 
    - Vertex const. fit
  - $0.5 < r < 30$  cm for  $K_S$  vertex
  - Electron veto for hadrons
    - Remove Bhabha BG with shower
  - $E_\gamma > 0.3$  for eta daughters
- Tag side
  - Lepton tag
  - $N_\gamma < 3$

