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# Measurement of $\tau^- \rightarrow K^- \pi^+ \pi^- \nu_\tau$ branching ratio at BELLE

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MyeongJae Lee  
(Seoul National University, Korea)

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# Introduction

- $\tau^- \rightarrow K^- \pi^+ \pi^- \nu$  decay
    - Hadronic tau decays with kaons provide a good probe of strange sector of weak charged current.
    - Cabibbo-suppressed decay
    - Contribution to strange spectral function, strange quark mass and  $V_{us}$
    - Possible resonance
      - $K_1(1270) \rightarrow K^*(892)\pi$ ,  $K^*(892) \rightarrow K\pi$  (42% ?)
      - $K_1(1270) \rightarrow K\rho(770)$ ,  $\rho(770) \rightarrow \pi\pi$  (16% ?)
      - $K_1(1400) \rightarrow K^*(892)\pi$ ,  $K^*(892) \rightarrow K\pi$  (>40% ?)
    - All these requires BR and invariant mass distribution study.
  - Main Background :
    - $\tau \rightarrow \pi\pi^+\pi^-\nu_\tau$ , (BR = 9.33%),  $\tau \rightarrow KK\pi\nu_\tau$  (BR = 0.153%),  
 $\tau \rightarrow KK_s\nu_\tau$  (BR = 0.077%)
    - Kaon identification is the most important in this analysis, because of large branching ratio of  $\tau \rightarrow \pi\pi^+\pi^-\nu_\tau$
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- Four 3-prong modes should be measured simultaneously.

# KEKB/Belle experiment

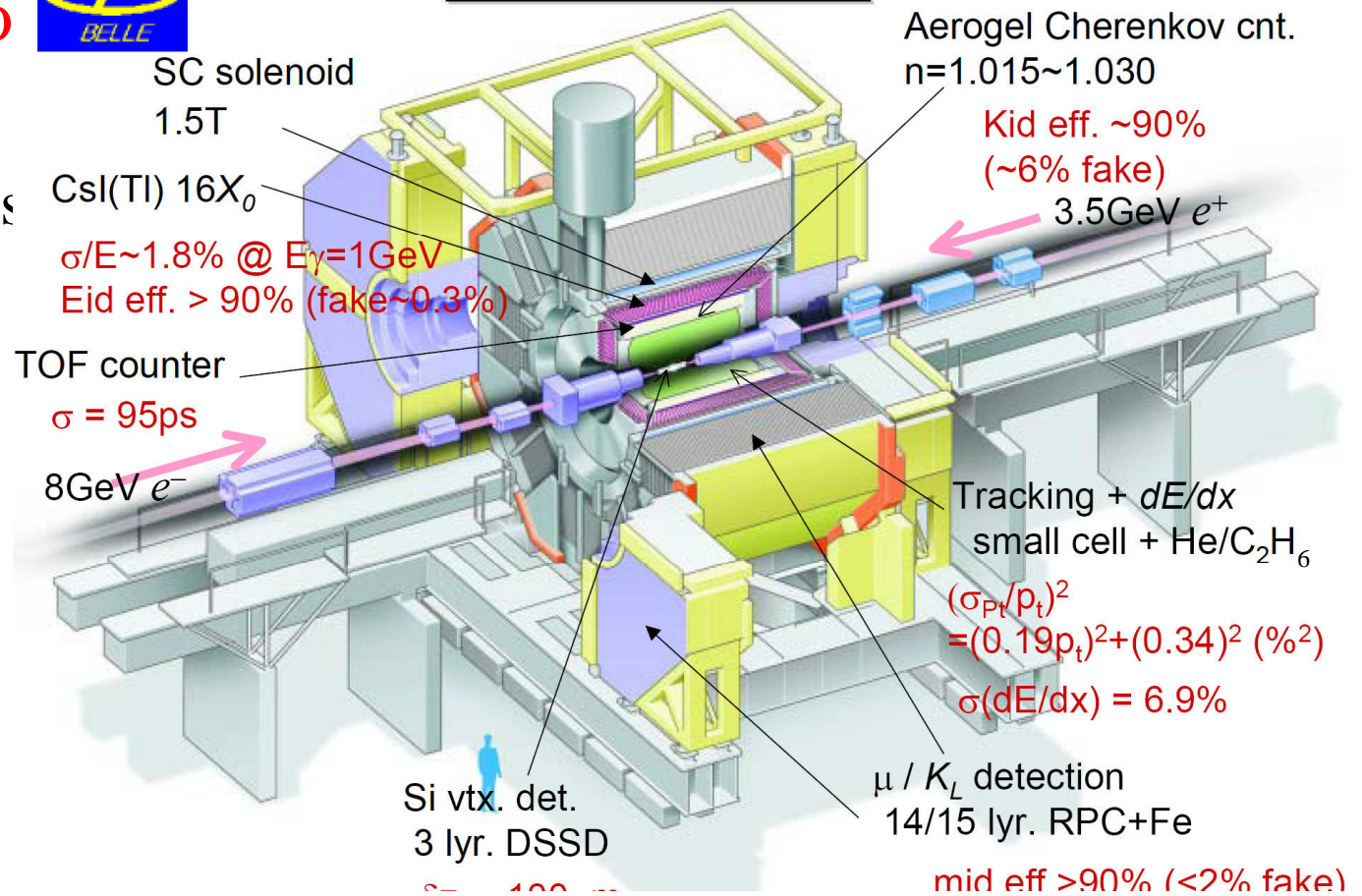


## High intensity $e^+e^-$ collider on Y(4S)

- World highest luminosity of  $1.7 \times 10^{34}/\text{cm}^2/\text{s}$
- Similar cross-section with BB ( $\sim 0.9\text{nb}$ )  
→  $\tau$ -factory!
- Good PID ability and vertex resolution



## Belle Detector



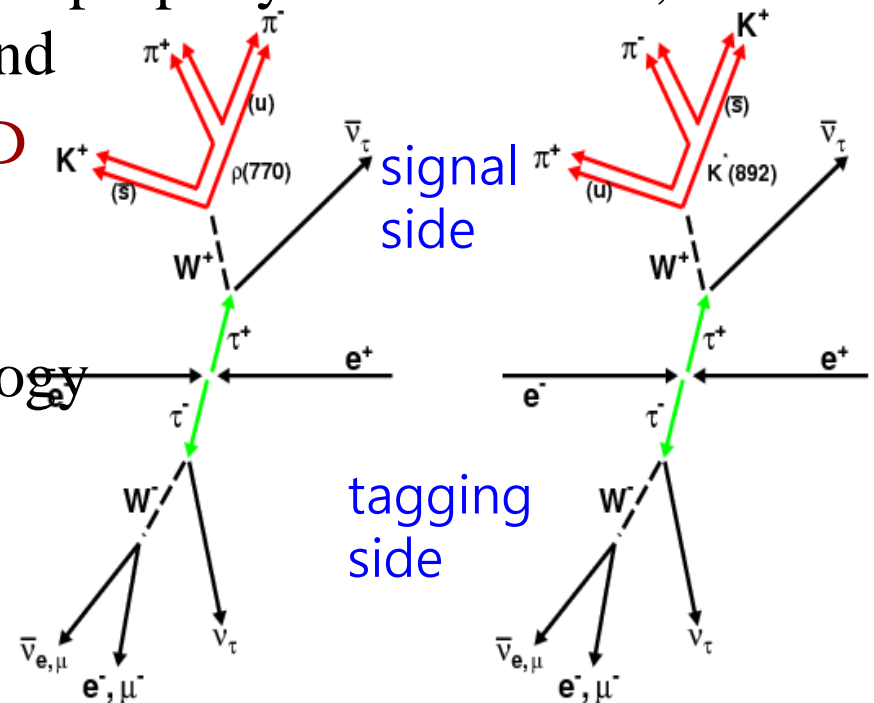
# Event selection for $\tau \rightarrow hhh\nu$

## 1. Tau candidate selection

- **Number of charged track = 4** and **sum of charge = 0**, with proper Calorimeter energy, vertex, and transverse momentum requirement

## 2. Background suppression

- Require missing momentum should be properly reconstructed, to suppress  $2\text{-}\gamma$  and  $q\text{-}q\text{-bar}$  background
- **Tight likelihood ratio cut for Kaon ID**
- Select a event with one  $e$  or  $\mu$ , and three  $K$  or  $\pi$
- Event shape : thrust, **3-1 prong topology**
- Invariant mass cut : require tau mass range



### 3. Final event selection

- No  $K_s$ ,  $\pi^0$ , energetic gamma candidate

: signal  
 : BG

| Cuts                 | Efficiency (N(passed) / N(total)) |                              |                                   |                         |
|----------------------|-----------------------------------|------------------------------|-----------------------------------|-------------------------|
|                      | $\tau \rightarrow K\pi\pi\nu$     | $\tau \rightarrow K_s\pi\nu$ | $\tau \rightarrow \pi\pi\pi^0\nu$ | $e^+e^- \rightarrow qq$ |
| tau pair selection   | <b>0.77</b>                       | <b>0.63</b>                  | <b>0.78</b>                       |                         |
| N(trk) = 4           | <b>0.53</b>                       | <b>0.16</b>                  | <b>0.51</b>                       | <b>0.20</b>             |
| Missing mass         | <b>0.45</b>                       | $8.5 \times 10^{-2}$         | <b>0.43</b>                       | <b>0.13</b>             |
| PID                  | <b>0.33</b>                       | $6.1 \times 10^{-2}$         | <b>0.33</b>                       | $8.3 \times 10^{-3}$    |
| Thrust cut/3-1 prong | <b>0.31</b>                       | $5.7 \times 10^{-2}$         | <b>0.30</b>                       | $6.9 \times 10^{-4}$    |
| Inv. mass cut        | <b>0.30</b>                       | $5.6 \times 10^{-2}$         | <b>0.29</b>                       | $2.9 \times 10^{-4}$    |
| N( $K_s$ ) = 0       | <b>0.30</b>                       | $2.0 \times 10^{-2}$         | <b>0.29</b>                       | $2.6 \times 10^{-4}$    |
| N( $\pi^0$ ) = 0     | <b>0.28</b>                       | $1.8 \times 10^{-2}$         | <b>0.14</b>                       | $6.6 \times 10^{-5}$    |
| N( $\gamma$ ) = 0    | <b>0.28</b>                       | $1.8 \times 10^{-2}$         | <b>0.06</b>                       | $4.0 \times 10^{-5}$    |

$\tau \rightarrow hhh\nu$   
 selection  
 efficiency

In  $\tau \rightarrow K\pi\pi\nu$   
real data

- qq events ratio : 0.84%**
- Two photon events ratio : 0.12%**

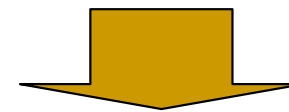
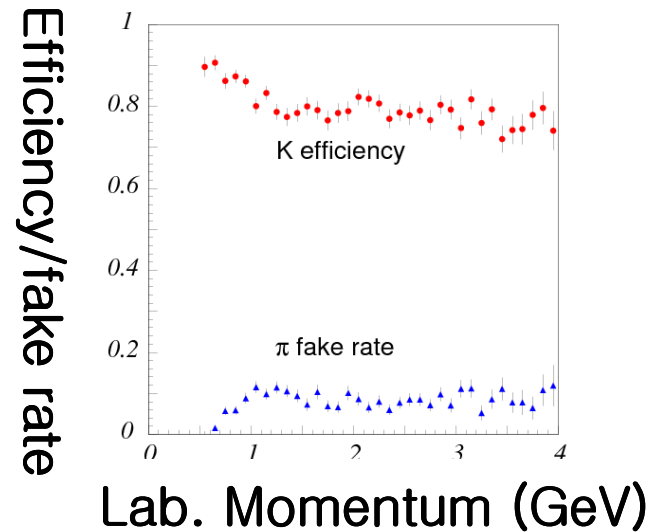
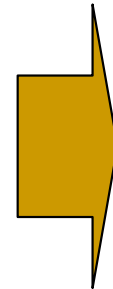
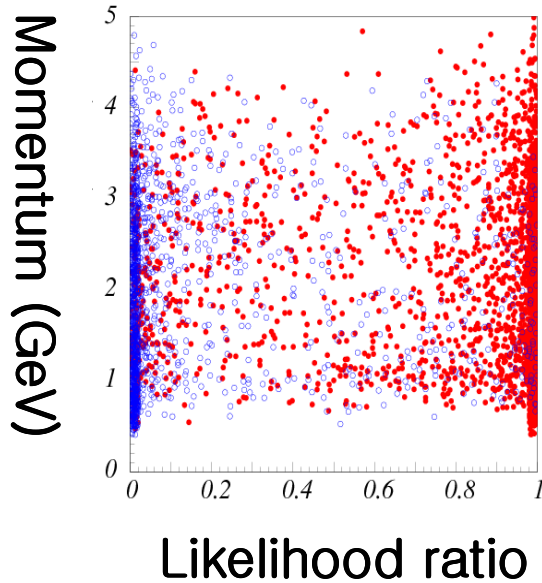


Suppressed sufficiently!

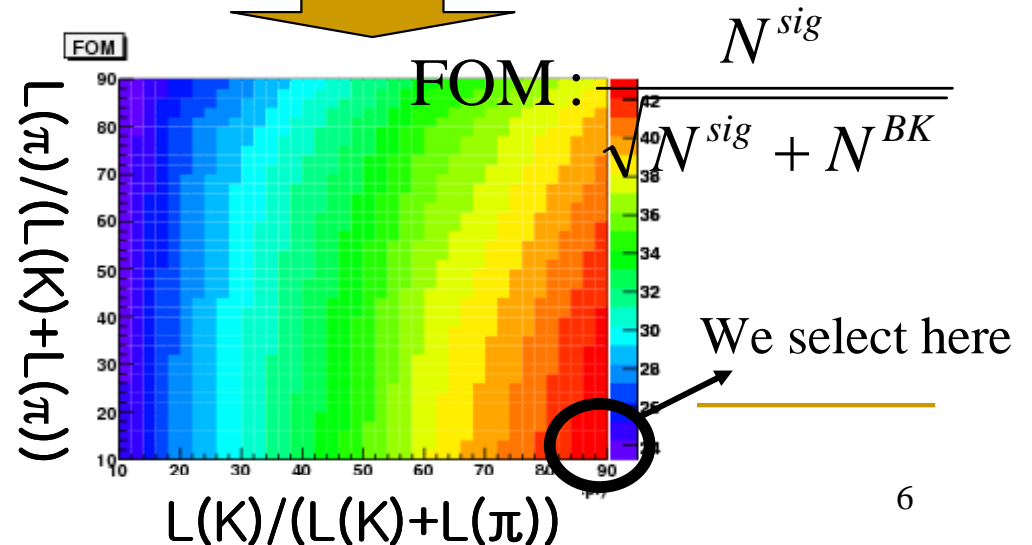
# K/ $\pi$ separation

Used  $dE/dx$ , Cherenkov angle,  
and time of flight for  
K/ $\pi$  Likelihood ratio :  $L(K)/(L(K)+L(\pi))$

Used  $D^{*+} \rightarrow D^0(\rightarrow K^-\pi^+) \pi^+$  to  
measure efficiency, fake rate  
and their systematics



Construct figure of merit to select best  
cut for Kaon ID likelihood ratio,  
When signal :  $K\pi\pi$  decay  
Background :  $\pi\pi\pi$ ,  $KK\pi$  decay



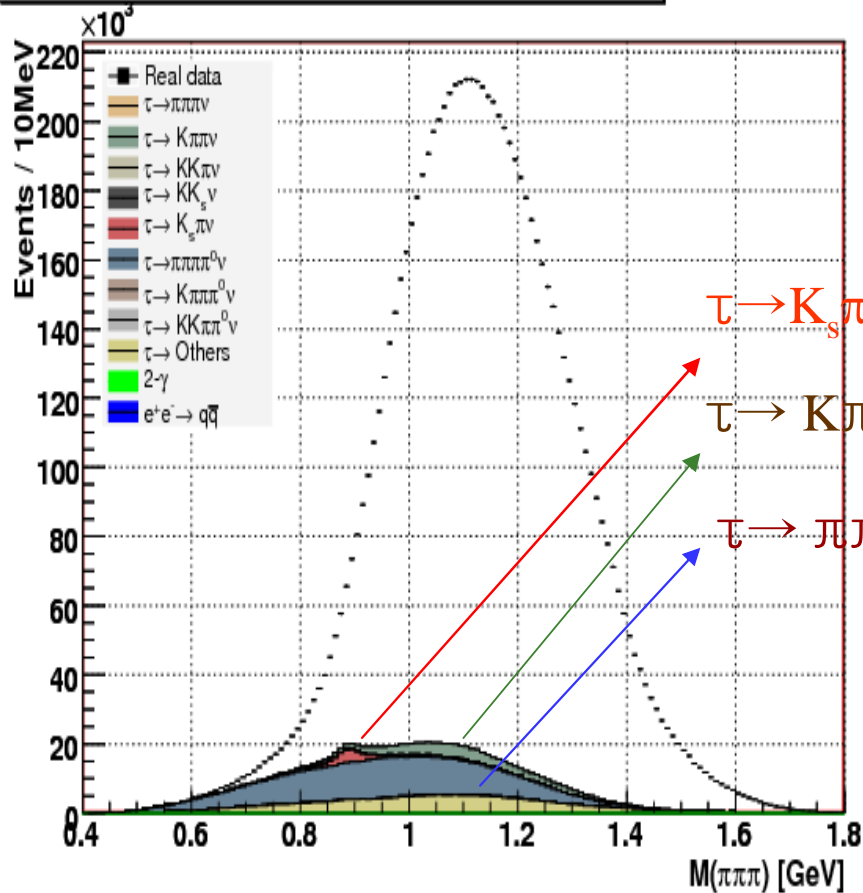
# Data



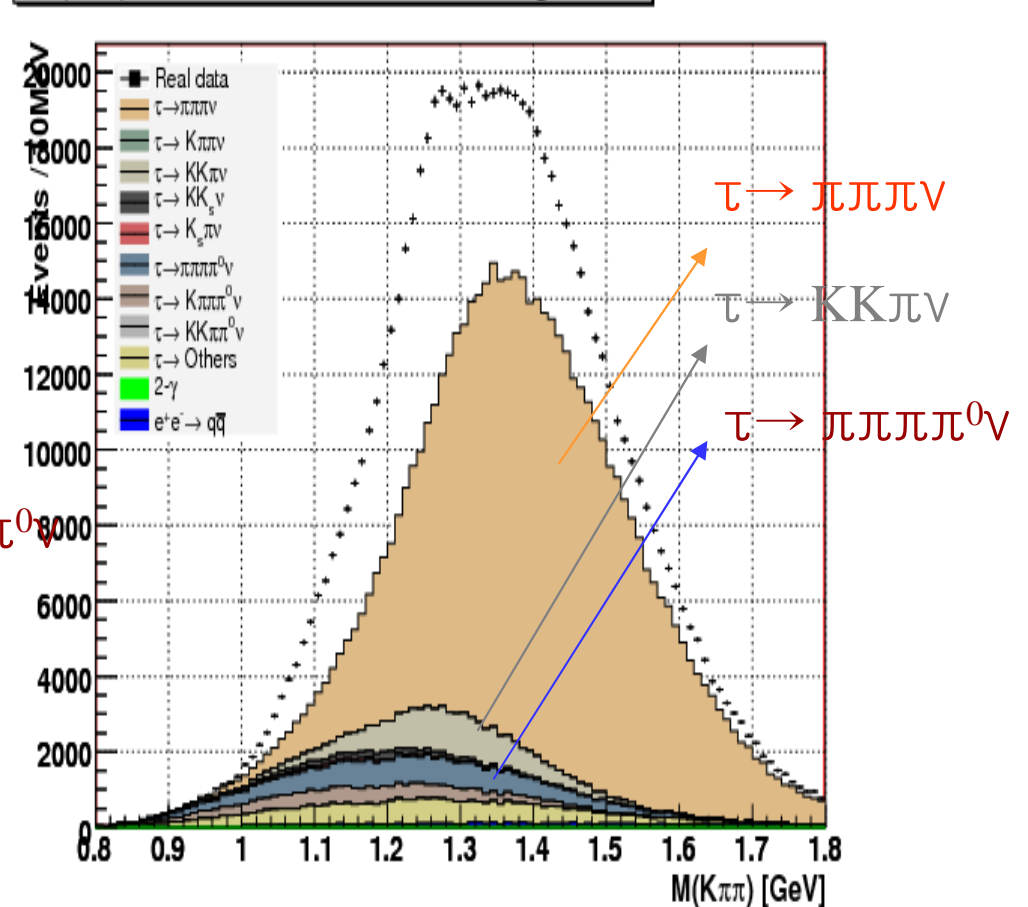
- Tau candidate with **668.9** fb<sup>-1</sup> collected by BELLE detector (615M  $\tau\tau$  pair)
- Tau generic MC generated by KKMC and TAUOLA package :  $\sim 1340$  fb<sup>-1</sup>

# Comparison of $M_{INV}$ distribution of $\tau^- \rightarrow \pi^- \pi^+ \pi^- \nu$ , $\tau^- \rightarrow K^- \pi^+ \pi^- \nu$

$M(\pi\pi\pi)$  for  $\tau \rightarrow \pi\pi\pi\nu$ , with stacked background



$M(K\pi\pi)$  for  $\tau \rightarrow K\pi\pi\nu$ , with stacked background



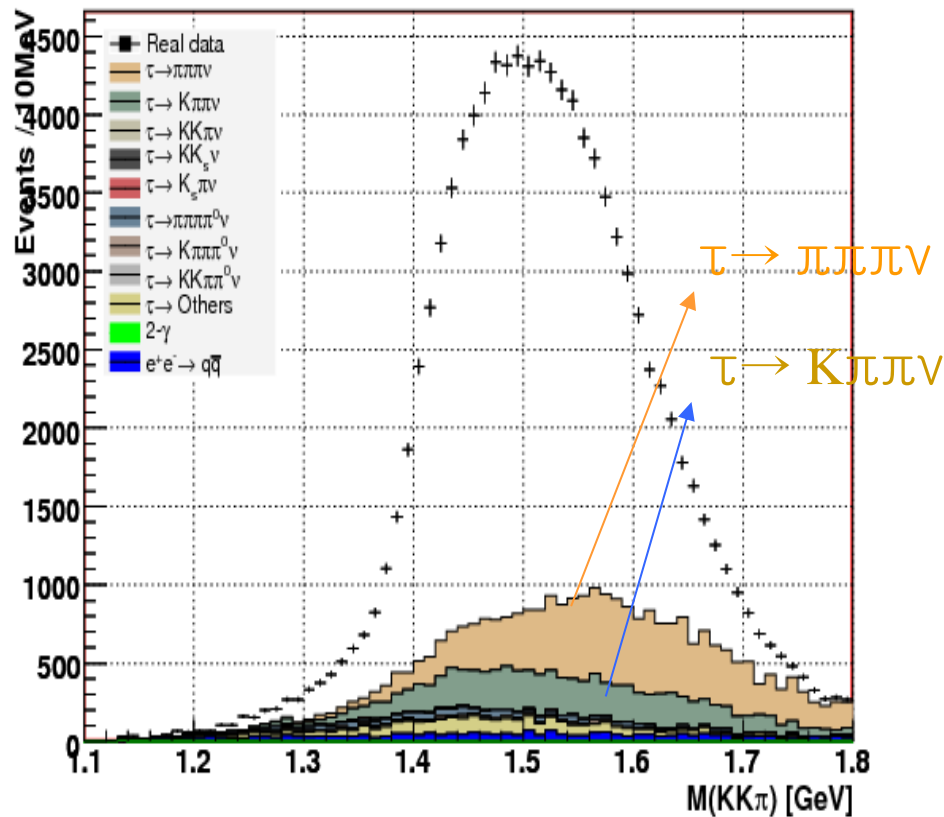
Black point : real data

Colored (stacked) histogram : background estimated from MC

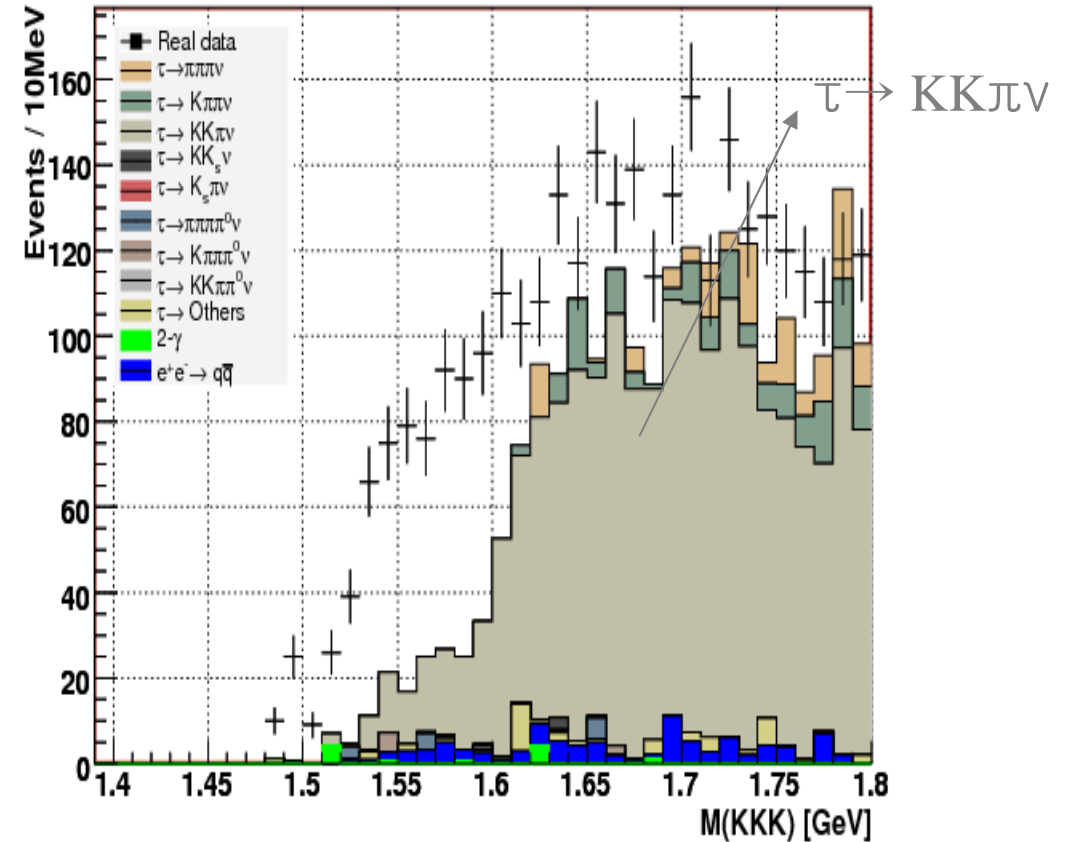


# Comparison of $M_{INV}$ distribution of $\tau^- \rightarrow K^- K^+ \pi^- \nu$ , $\tau^- \rightarrow K^- K^+ K \pi^- \nu$

$M(KK\pi)$  for  $\tau \rightarrow KK\pi\nu$ , with stacked background



$M(KKK)$  for  $\tau \rightarrow KKK\nu$ , with stacked background



Black point : real data

Colored (stacked) histogram : background estimated from MC

# Branching ratio calculation

$$N_i^{true} = \epsilon^{-1}_{ij} N_j^{rec}$$

$N_i^{true}$  : Number of true event for i-th mode

$N_i^{rec}$  : Number of reconstructed event for i-th mode

$\epsilon$  : efficiency migration matrix

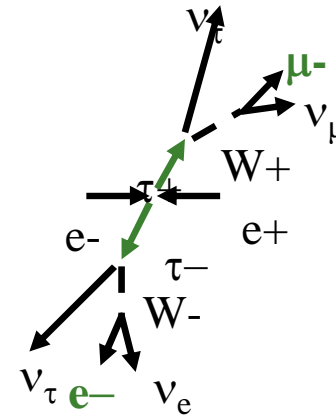
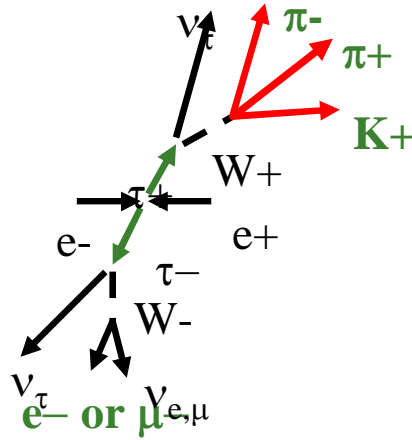
## Efficiency migration matrix $\epsilon$ (%)

| rec \ true                   | $\tau \rightarrow \pi\pi\nu$ | $\tau \rightarrow K\pi\nu$ | $\tau \rightarrow KK\pi\nu$ | $\tau \rightarrow KKK\nu$ |
|------------------------------|------------------------------|----------------------------|-----------------------------|---------------------------|
| $\tau \rightarrow \pi\pi\nu$ | 23.0                         | 7.6                        | 2.3                         | 0.73                      |
| $\tau \rightarrow K\pi\nu$   | 1.2                          | 17.2                       | 4.9                         | 2.3                       |
| $\tau \rightarrow KK\pi\nu$  | $4.0 \times 10^{-2}$         | 0.47                       | 12.9                        | 6.0                       |
| $\tau \rightarrow KKK\nu$    | $2.8 \times 10^{-4}$         | $1.4 \times 10^{-2}$       | 0.28                        | 9.4                       |

- Efficiency : 10 ~ 20%
- Fake rate from  $\pi\pi$  to  $K\pi$  is sufficiently small

# Normalization by $(\tau \rightarrow e\nu\nu; \tau \rightarrow \mu\nu\nu)$

Normalized by a event that one tau decay to  $\tau \rightarrow e\nu\nu$   
and the other tau decay to  $\tau \rightarrow \mu\nu\nu$



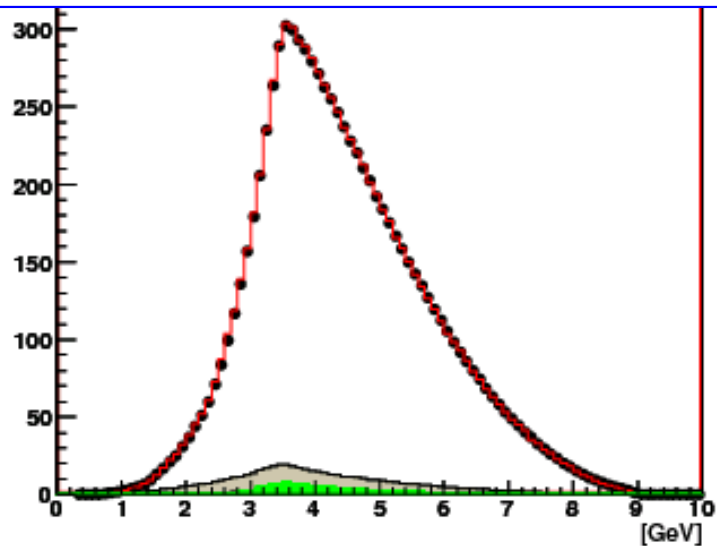
$$Br_{\tau \rightarrow K\pi\pi\nu} = \frac{N_{Sig, K\pi\pi}}{2N_{\tau\tau} \epsilon_{K\pi\pi} (Br_{\tau \rightarrow e\nu\nu} + Br_{\tau \rightarrow \mu\nu\nu})}$$

$$Br_{\tau \rightarrow e\nu\nu} \times Br_{\tau \rightarrow \mu\nu\nu} = \frac{N_{Sig, e\mu}}{2N_{\tau\tau} \epsilon_{e\mu}}$$

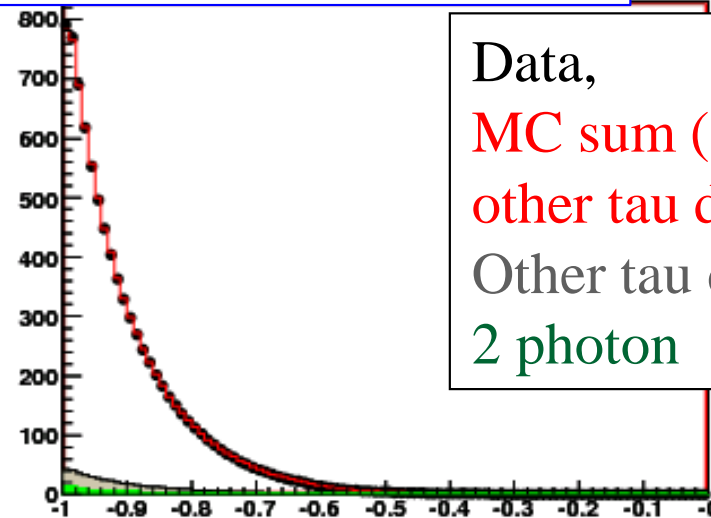
$$\Rightarrow Br_{\tau \rightarrow K\pi\pi\nu} = \frac{N_{sig, K\pi\pi} \cdot \epsilon_{e\mu}}{N_{sig, e\mu} \cdot \epsilon_{K\pi\pi}} \cdot \frac{Br_{\tau \rightarrow e\nu\nu} \cdot Br_{\tau \rightarrow \mu\nu\nu}}{Br_{\tau \rightarrow e\nu\nu} + Br_{\tau \rightarrow \mu\nu\nu}}$$

Need precise measurement

$\sqrt{(E_e + E_\mu)^2 - (\vec{p}_e + \vec{p}_\mu)^2}$  distribution



$\cos(e, \mu)$  distribution



Data,  
 MC sum ((e;μ) signal MC +  
 other tau decay + 2 photon)  
 Other tau decay,  
 2 photon

⇒ Extract ( $\tau \rightarrow e\nu\nu; \tau \rightarrow \mu\nu\nu$ ) event number  
 by subtracting MC background from data



# List of systematic errors

|                                     | $\tau \rightarrow$<br>$\pi\pi\pi\nu$ | $\tau \rightarrow$<br>$K\pi\pi\nu$ | $\tau \rightarrow$<br>$KK\pi\nu$ | $\tau \rightarrow$<br>$KKK\nu$ |
|-------------------------------------|--------------------------------------|------------------------------------|----------------------------------|--------------------------------|
| Track find eff.                     | 3.2                                  | 3.2                                | 3.2                              | 3.1                            |
| Eff. mig. matrix<br>(including PID) | 1.5                                  | 1.7                                | 1.9                              | 2.3                            |
| Trigger eff.                        | 0.5                                  | 0.5                                | 0.6                              | 0.6                            |
| Luminosity                          | 0.1                                  | 0.1                                | 0.1                              | 0.1                            |

- Track finding efficiency : estimated from  $D^{*+} \rightarrow \pi D^0$ ,  $D^0 \rightarrow \pi\pi K_s$ ,  $K_s \rightarrow \pi^+\pi^-$
- Lepton ID error : estimated from  $\gamma\gamma \rightarrow ee/\mu\mu$
- Kaon ID error : estimated from  $D^{*+} \rightarrow D^0\pi_s^+$ ,  $D^0 \rightarrow K^-\pi^+$
- Trigger efficiency :  $\sim 86 \pm 0.6\%$
- Luminosity error :  $668.9 \text{ fb}^{-1} \pm 1.4\%$



|               | $\tau \rightarrow$<br>$\pi\pi\pi\nu$ | $\tau \rightarrow$<br>$K\pi\pi\nu$ | $\tau \rightarrow$<br>$KK\pi\nu$ | $\tau \rightarrow$<br>$KKK\nu$ |
|---------------|--------------------------------------|------------------------------------|----------------------------------|--------------------------------|
| Gamma veto    | 0.8                                  | 2.5                                | 1.1                              | 1.0                            |
| BF correction | 0.3                                  | 2.0                                | 0.2                              | 0.3                            |
| Lep. decay BF | 0.2                                  | 0.2                                | 0.2                              | 0.2                            |
| Total (%)     | 3.7                                  | 4.9                                | 3.9                              | 4.0                            |

- Gamma veto : Number of energetic gamma and its energy are changed
- BF correction : The error of generator level branching fraction from other modes
- Leptonic decay branching fraction :  $0.352 \pm 0.001$

**~ 4% for all modes. The track finding efficiency error is dominant.**



# Result on branching ratio

(Preliminary result )

|  | Branching ratio  | Br (PDG2008)                     |
|--|--|----------------------------------|
| $\tau^- \rightarrow \pi^- \pi^+ \pi^- \nu$ | $(8.41 \pm 0.00(\text{st.})^{+0.32}_{-0.30}(\text{sy.})) \times 10^{-2}$ | $(9.03 \pm 0.06) \times 10^{-2}$ |
| $\tau^- \rightarrow K^- \pi^+ \pi^- \nu$   | $(3.25 \pm 0.02(\text{st.})^{+0.16}_{-0.15}(\text{sy.})) \times 10^{-3}$ | $(2.87 \pm 0.16) \times 10^{-3}$ |
| $\tau^- \rightarrow K^- K^+ \pi^- \nu$     | $(1.53 \pm 0.01(\text{st.})^{+0.06}_{-0.06}(\text{sy.})) \times 10^{-3}$ | $(1.40 \pm 0.05) \times 10^{-3}$ |
| $\tau^- \rightarrow K^- K^+ K^- \nu$       | $(2.60 \pm 0.23(\text{st.})^{+0.10}_{-0.10}(\text{sy.})) \times 10^{-5}$ | $(1.58 \pm 0.18) \times 10^{-5}$ |

Cf) CLEO result (2003)

|  | Branching ratio   |
|--|---|
| $\tau^- \rightarrow \pi^- \pi^+ \pi^- \nu$ | $(9.13 \pm 0.05(\text{st.}) \pm 0.46(\text{sy.})) \times 10^{-2}$ |
| $\tau^- \rightarrow K^- \pi^+ \pi^- \nu$   | $(3.84 \pm 0.14(\text{st.}) \pm 0.38(\text{sy.})) \times 10^{-3}$ |
| $\tau^- \rightarrow K^- K^+ \pi^- \nu$     | $(1.55 \pm 0.06(\text{st.}) \pm 0.09(\text{sy.})) \times 10^{-3}$ |
| $\tau^- \rightarrow K^- K^+ K^- \nu$       | $< 3.7 \times 10^{-5} @ 90\%$                                     |



# Summary

- Hadronic tau decays to final states with three charged hadrons are studied with  $\sim 5 \times 10^8$   $\tau$ -pair decays.
- Evaluate BR of  $\tau^- \rightarrow K^- \pi^+ \pi^- \nu$ ,  $\tau^- \rightarrow K^- K^+ \pi^- \nu$ ,  $K^- K^+ K^- \nu$ , simultaneously
  - $B(\tau^- \rightarrow K^- \pi^+ \pi^- \nu) = (3.25 \pm 0.02^{+0.16}_{-0.15}) \times 10^{-3}$ 
    - $B(\tau^- \rightarrow \pi^- \pi^+ \pi^- \nu) = (8.41 \pm 0.00(\text{st.})^{+0.32}_{-0.30}(\text{sy.})) \times 10^{-2}$
    - $B(\tau^- \rightarrow K^- K^+ \pi^- \nu) = (1.53 \pm 0.01^{+0.06}_{-0.06}) \times 10^{-3}$
    - $B(\tau^- \rightarrow K^- K^+ K^- \nu) = (2.60 \pm 0.23^{+0.10}_{-0.10}) \times 10^{-5}$
  - Selected proper event selection criteria for PID, and (e; $\mu$ ) normalization : To reduce the systematic error
  - Consistent with CLEO result, inconsistent with recent PDG (which is contributed largely by the most recent precise measurement from BABAR) and higher systematic error level than BABAR result.